The background is a solid purple color. On the left side, there are two white zigzag lines stacked vertically. Below them is a light purple semi-circle. At the bottom left, there is a yellow circle with a white outline. On the right side, there is a large yellow semi-circle at the bottom. The main content is enclosed in a white double-line rectangular border.

# Week 3 Tutorial

Tutorial Section  
Tutorial Time  
Tutorial TA Name

# About Me

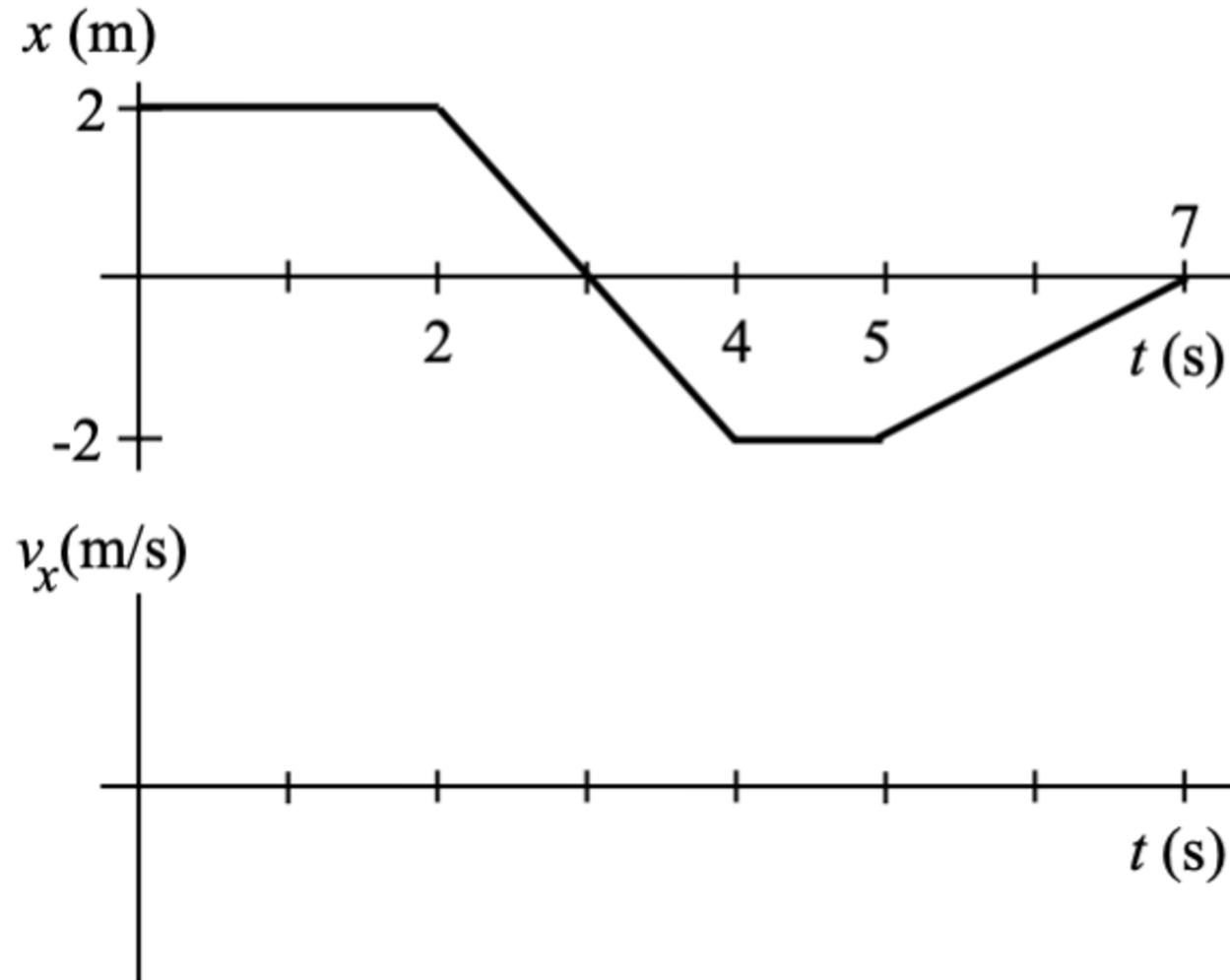
# Tutorial Structure

- Introduction
- Question 1
- Problem Solving Framework
- Question 2
- Problem Solving Framework
- Q&A

# Question 1

A position vs. time graph is shown. On the velocity versus time graph below it sketch the corresponding velocity as a function of time. Show all calculations, and label the axes appropriately.

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# Problem Solving Framework

PHYSICAL REVIEW PHYSICS EDUCATION RESEARCH **16**, 010123 (2020)

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**Template for teaching and assessment of problem solving in introductory physics**

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A. V. Fritz<sup>4</sup> , and C. E. Wieman<sup>1,3</sup> 

# 1. Framing

Visual Representation

Assumptions and Simplifications

Relevant Concepts

Information Needed

Similar Problems

# 2. Planning

Solution Plan

Rough Estimate

# 3. Execution

Carry-out Plan for solving

- Work in algebra/symbols until the BITTER end
- Plug in numbers at the LAST step

# 4. Answer Checking

Compare to Estimate

Units Check

Limits Test

Getting (UnStuck)

1. Framing

2. Planning

3. Execution

4. Answer Checking

# 1. Framing



Visual representation: describe the motion based on position vs time graph; i.e., from 0-2s, position  $x$  stays the same at 2m.



Assumptions and simplifications: Only consider this motion in 1D.



Relevant concept: the relationship between position  $x$ , velocity  $V_x$ :  $V_x = dx/dt$



Information needed: position change during certain time period



Similar problems: given  $V_x$  vs  $t$  graph, draw  $a_x$  vs  $t$  graph; given  $V_x$  vs  $t$  graph, draw  $x$  vs  $t$  graph, etc.

## 2. Planning

- Rough estimate: It's hard to estimate how a graph should look like but we know that once the slope of  $x$  vs  $t$  graph changes the velocity would change. So, in this problem we need to calculate velocity for each time section separately. Also, roughly we can estimate the sign of velocity (positive/negative/0) from visually viewing the graph. We can do that for final double check.
- Solution plan: First divide 0-7s into several time section for separate velocity calculation. Then calculate velocity using  $V_x = dx/dt$  for each time section. Finally draw line to represent velocity during each period of time.

# 3. Execution

- See solution on slide 10. Carry out the calculation, plug in the numbers at the last step.

## 4. Answer Checking

Compare to estimates: compare the calculation results to your rough estimates see whether the sign matches.

Units: Think about what unit we use for  $V_x$  in this problem and add them in your final answer.

Limits: Think about how  $x$  vs  $t$  graph looks like with 0 velocity? How increasing or decreasing the velocity change  $x$  vs  $t$  graph?

Getting (UnStuck)? Not sure what it means...

# Solution

2. A position vs. time graph is shown. On the velocity versus time graph below it sketch the corresponding velocity as a function of time. Show all calculations, and label the axes appropriately.

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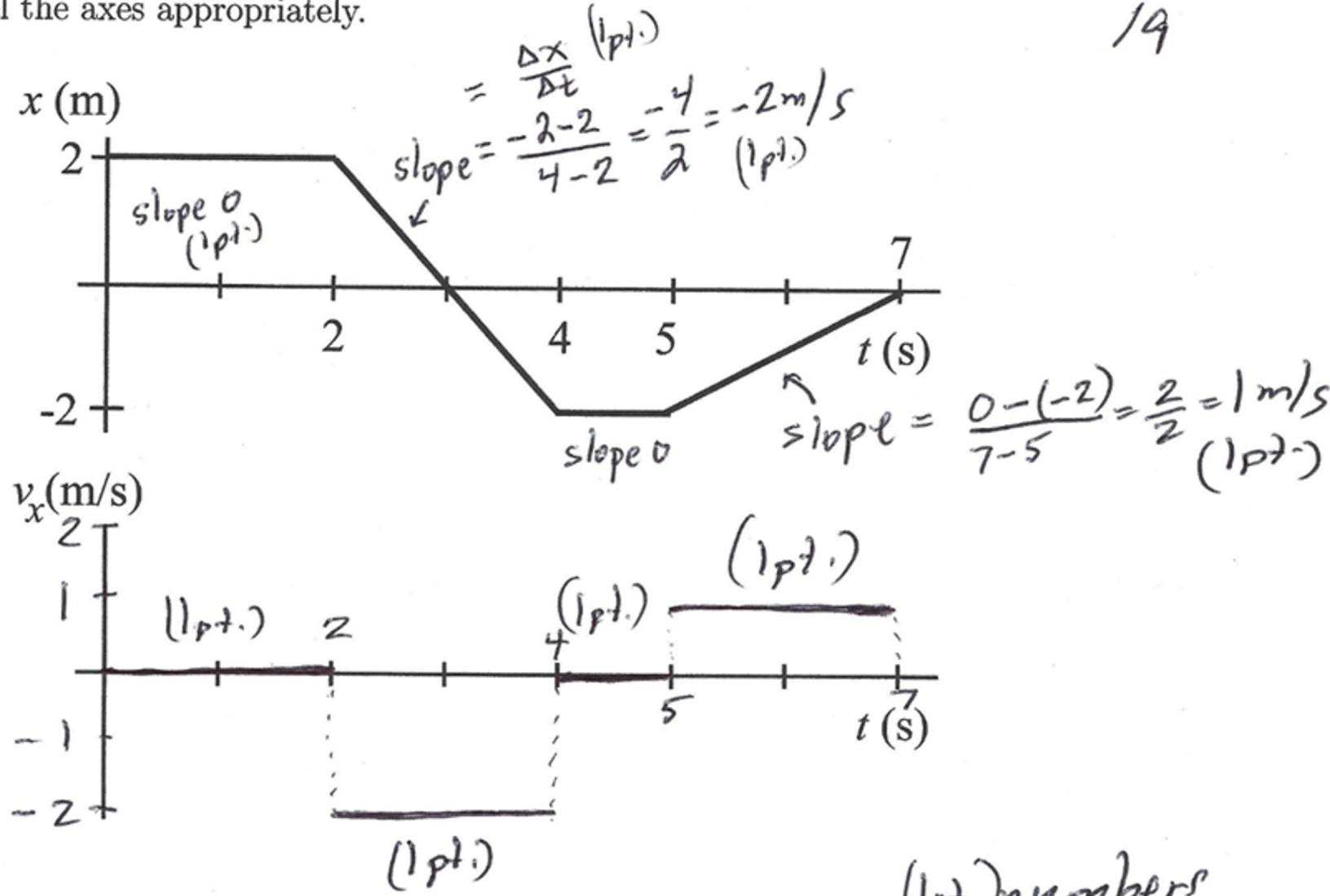


FIG. 1:

(1pt.) numbers on axes

## Question 2

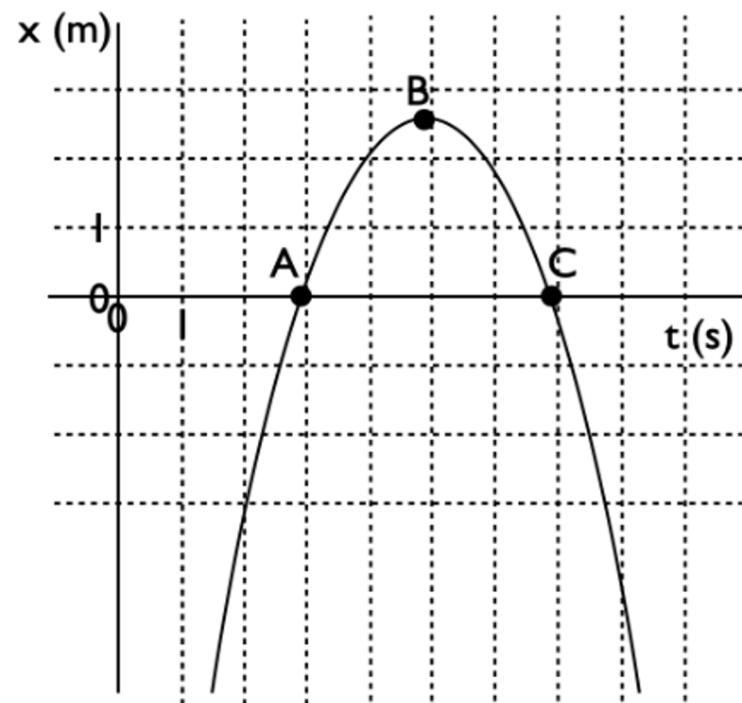


FIG. 1:

3. (a) At each of A, B and C on Fig. 1, estimate the x-component of the velocity vector,  $v_x$  from the position vs. time graph ( /3) . Draw a tangent line to the graph at each location ( /3) and show the calculation of its slope ( /3).

(b) What sign, if any, does the x-component of the acceleration vector,  $a_x$ , have at point B ( /2)?

1. Framing

2. Planning

3. Execution

4. Answer Checking

# 1. Framing



Visual representation: describe the motion based on position vs time graph; i.e., from 0-2s, position  $x$  stays the same at 2m.



Assumptions and simplifications: Only consider this motion in 1D.



Relevant concept: the relationship between position  $x$ , velocity  $V_x$ :  $V_x = dx/dt$



Information needed: position change during certain time period



Similar problems: given  $V_x$  vs  $t$  graph, draw  $a_x$  vs  $t$  graph; given  $V_x$  vs  $t$  graph, draw  $x$  vs  $t$  graph, etc.

## 2. Planning

- Rough estimate: We can estimate the sign of velocity (positive/negative/0) from visually viewing the graph, and relative change velocity based on the slope.
- Solution plan: For a, at each point, draw the tangent line and calculate velocity using  $V=dx/dt$ . For b, use  $a=dV/dt$  to estimate the sign.

## 3. Execution

- See solution above. Carry out the calculation, plug in the numbers at the last step.

## 4. Answer Checking

Compare to estimates: compare the calculation results to your rough estimates see whether the sign matches.

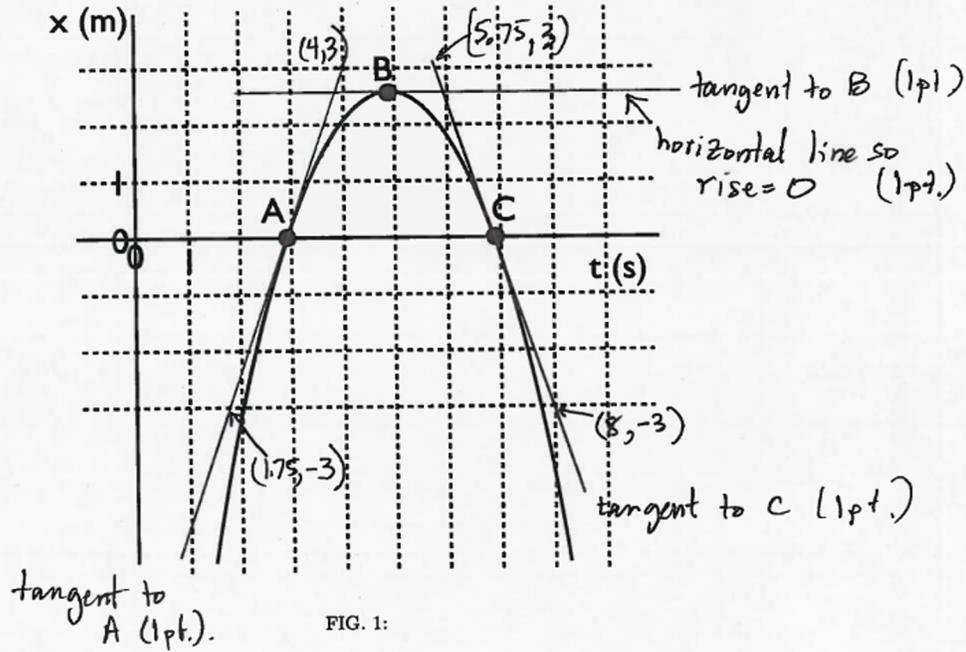
Units: Think about what unit we use for  $V_x$  in this problem and add them in your final answer.

Limits: Think about how  $x$  vs  $t$  graph looks like with 0 velocity? How increasing or decreasing the velocity change  $x$  vs  $t$  graph?

Getting (UnStuck)? Not sure what it means...

# Solution

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3. (a) At each of A, B and C on Fig. 1, estimate the x-component of the velocity vector,  $v_x$  from the position vs. time graph (/3). Draw a tangent line to the graph at each location (/3) and show the calculation of its slope (/3).

$$v_{Ax} = \frac{\Delta x}{\Delta t} = \frac{3 - (-3)}{4 - 1.75} \text{ m/s} \quad (1 \text{ pt.})$$

$$= \frac{6}{2.25} \text{ m/s}$$

$$= 2.7 \text{ m/s} \quad (1 \text{ pt.})$$

$$v_{Bx} = \frac{0}{0} = 0 \text{ m/s} \quad (1 \text{ pt.})$$

$$v_{Cx} = \frac{\Delta x}{\Delta t} = \frac{-3 - 3}{8 - 5.75} \text{ m/s} = \frac{-6}{2.25} \text{ m/s} = -2.7 \text{ m/s} \quad (1 \text{ pt.})$$

note: looks symmetric - be lenient with values accepted

(b) What sign, if any, does the x-component of the acceleration vector,  $a_x$ , have at point B (/2)?

$a_x$  has a negative sign (at B) since  $v_x$  is positive just before B and negative just after B.  
 either (1pt.)  
 ie.  $a_x = \frac{v_{Cx} - v_{Ax}}{t_C - t_A} < 0$